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ESTIMATING GERMANY’S POTENTIAL OUTPUT
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January 2007

Abstract

Potential output measures a country’s attainable aggregate living standard and is thus one of the most important categories of economics. It is also a key indicator for monetary and fiscal policy. Despite its prominence, however, potential output is a difficult concept to pinpoint both theoretically and even more so empirically. The article discusses the reasons for the marked revisions of potential output estimates by major international organizations. We then present the results of our attempts to quantify Germany’s potential output based on a production function approach coupled with the Kalman-filter technique to estimate the NAIRU. We find that potential output and potential output growth greatly depend on how the NAIRU and potential total factor productivity are modelled. Given the difficulties involved in robustly estimating potential output, especially in real time, economic policy makers need to learn to pursue their policy objectives without reference to this variable.

1. Introduction

Potential output measures a country’s attainable aggregate living standard and is thus one of the most important categories of economics. It is also a key indicator for monetary and fiscal policy. The ECB, for example, uses the output gap – the relative difference between potential output and GDP – as a leading indicator of inflation and requires a precise growth rate of potential output to determine its reference value for M3. Potential output is also relevant for fiscal policy and medium-term fiscal planning, to determine, for example, the structural budget deficit. Despite its prominence, however, potential output is a difficult concept to pinpoint both theoretically and even more so empirically.

In this article we present the results of our attempts to quantify Germany’s potential output. Section 2 highlights the theoretical difficulties of unambiguously defining potential out-
put. Section 3 discusses the reasons for the marked revisions of potential output estimates by major international organizations. Section 4 then presents our own estimates of Germany’s potential output using a production function approach coupled with the Kalman-filter technique to estimate the NAIRU. We find that potential output and potential output growth greatly depends on how the NAIRU and total factor productivity are modelled. In section 5 policy conclusions are drawn from the resulting inexactness and unreliability of potential output estimates.

In the literature the unreliability of real time potential output estimates became a topic of research beginning at the turn of the decade, pioneered by Orphanides (1998) and Smets (1998). Döpke (2004) examines the problem using German data. They attribute the unreliability to the endpoint problem, as do we. Our focus is slightly different, however, as we attempted to mitigate the endpoint problem by estimating the crucially important total factor productivity (TFP) using an equation rather than a filtering method or trend estimate. Similar TFP estimates can be found in the literature (for example Denis et al. 2004: 47-48). Unfortunately we find that this modification does not reduce the unreliability of potential output estimates by much; nor does the inclusion of exogenous variables when estimating the NAIRU. However, again the focus is different, as we are concerned with the unreliability or arbitrariness of the estimates. The same applies to our NAIRU estimate, which is not a novelty, despite the use of exogenous variables. NAIRUs have been estimated by all international organizations (see, for example Denis et al. 2002, Turner et al. 2001 and International Monetary Fund 2001). Our resulting scepticism concerning potential output estimates does not lead us to advocate the difference rule suggested by Orphanides/Williams (2002) nor to advise that is better “to err on the side of caution” when using output gap estimates (European Commission 2002: 9). Rather we support Smets (1998) and others in arguing that uncertain output gap estimates should receive low or rather no weight in economic policy decisions. We argue that monetary policy — in order to remain preemptive — should rather focus on the development of wages costs and especially unit labour costs.

2. Potential output in a theoretical perspective

Potential output is the sustainable level of real (inflation-adjusted) GDP. It is constrained due to limited natural resources (population, raw materials), institutional factors (e.g. on labor markets) and the factor endowment (especially the capital stock and human capital). A given level of output is sustainable if it does not generate inflationary or deflationary tendencies. Arthur M. Okun, who coined the term potential output in 1962, defined it as the level production at full employment, the latter according to Okun referring to the degree of utilisation of the factors of production that does not cause inflationary pressure. In a market economy the concept of potential output necessarily implies an unemployment rate greater than zero. Therefore its analysis also requires analysis of this “equilibrium” unemployment rate, the
The NAIRU may be affected not only by institutional factors, but also by macroeconomic policy as indicated by the quote below.

“In some countries, such as the United States, the rise in unemployment was transitory; in others, including many European countries, the NAIRU rose and has remained high ever since. I argue that the reaction of policymakers to the early 1980s recessions largely explain these differences. ... In countries where unemployment rose permanently, it did so because policy remained tight in the face of the 1980s recessions.” (Ball 1999: 190)

The theoretical difficulties of unambiguously defining potential output are due to divergent opinions about the persistency of output gaps and the possible endogeneity of potential output, both of which arise from different assumptions about the inherent stability of the economy. From a Keynesian perspective the effectiveness of endogenous mechanisms that return the economy to a given equilibrium is uncertain at best. Longer-lasting negative output gaps are thus a likely occurrence and entail the danger of hysteretic effects causing potential output to adjust to the GDP rather than vice versa. In contrast, monetarists and proponents of new classical theory hold the view that the rational behaviour of economic agents rapidly corrects disequilibria and that potential output is unaffected by economic downswings and upswings. New Keynesians occupy a position somewhere in between. Economic policy advice differs in accordance with these divergent views. Whereas Keynesians tend to favour active macroeconomic stabilisation policies and regard macroeconomic policy as a necessary adjunct to structural reform, monetarists and new classical theorists view macro policy as

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2 The NAIRU concept was developed by Modigliani and Papademos (1975), who, however, called it NIRU (noninflationary rate of unemployment). The term NAIRU was first used by Tobin (1980). Unlike the term “natural rate of unemployment” introduced by Friedman in his Presidential Address to the American Economic Association in 1968, the NAIRU is not a purely neoclassical concept; see Carlin / Soskice (1990: 166).

more or less superfluous, argue strongly for rule-based policies, and consider structural reforms to be the key to higher economic growth.

An output gap that persists over a long period is unlikely from a theoretical perspective. Eventually capital stock adjustments (Bean 1997: 93; Gordon 1997: 439) and hysteresis on the labor markets\(^4\) will lower potential output until the gap disappears. Underutilization of capital is small if it exists at all and the long-term unemployed may not be hired at the going wage even if aggregate demand picks up. Since monetary policy is generally believed to be powerful enough to cause output gaps in the short and medium run, the implication for monetary policy is apparent: if output gaps close as a result of labor market hysteresis and capital stock adjustments, then macro policy is not neutral in the long run but rather affects the real economy.

“…If monetary policy can affect real economic activity by means other than money illusion then it may be possible for money to be nonsuperneutral in the long run.”

Espinosa-Vega (1998: 13)

In addition to the NAIRU, endogenous technological progress is a second channel through which macro policy may affect the level of potential output.

3. Revisions of Germany’s potential output

From an empirical perspective it is also the NAIRU and endogenous technological progress that make it difficult to estimate and forecast potential output with certainty. Volatile outcomes resulting from small changes in the specification or the estimation period pose a problem for policy makers because estimation errors can have dire consequences for unemployment and inflation.

Methods to estimate potential output can be categorised into three groups: first, purely statistical methods (eg. Hodrik-Prescott filter and Rotemberg filter); second, methods that determine potential output primarily on statistical grounds but make use of the interaction between certain economic variables (semi-structural methods, eg. multivariate Hodrick-Prescott filter and multivariate Kalman filter); and third, methods that determine potential output on the basis of economic factors (structural methods, eg. production function approach). Only structural methods make possible a distinction between different theoretical approaches. They are also better suited for projections and simulations exercises, especially in the case of changes in the structural or macroeconomic environment at the end of the observation period. They are superior to univariate methods because they provide an economic explanation of movements in potential output.

\(^4\) See Logeay/Tober (2006) for an overview of causes of labor market hysteresis.
In practice, however, estimates based on production functions are to a large extent based on univariate methods, especially the Hodrick-Prescott filter, to estimate the potential values of the individual components of the production function. It is therefore not surprising that the estimates of potential output of different institutions are quite similar and actually more similar than are the estimates of each institution for a specific year at different points in time. In the case of the International Monetary Fund (IMF) this difference can be exemplified best using the years 1999 and 2001. In the spring 2000 the IMF estimated Germany’s output gap in 1999 to be -2.8%; in the spring of 2006 the IMF puts the output gap in 1999 at +0.1%; this is not only a difference of almost 3 percentage points but also a change from negative to positive. The real-time estimate of Germany’s output gap in 2001, i.e. the estimate in the spring of 2002, was -1.2%; from today’s perspective (spring 2006) the IMF estimates the output gap in 2001 to have been 1.5% and thus markedly positive. An equally stark picture emerges when looking at the figures provided by the EU Commission and the OECD.\(^5\) Revisions of this magnitude invalidate the use of measures of output gaps and potential output growth as indicators for economic policy. To illustrate the problem we calculated Germany’s output gap for 2005 on the basis of the rate of potential growth that the IMF estimated in spring 2000 for period from 1992 to 2001, that is 2.1%.\(^6\) According to this calculation the output gap in 2005 would have exceeded 8%.\(^7\)

The frequent and large potential output revisions are largely due to the econometric methods used for estimating potential output, in particular the endpoint problem and forecast mistakes, rather than to data revisions or a changing view of underlying structural factors. Below we show how revisions come about by estimating the potential labor force, potential

\(^5\) See also Orphanides and Williams (2002) as well as Döpke (2004), who analyse this discrepancy between potential output estimates in real time and in retrospect for the United States and for Germany, respectively.

\(^6\) The potential growth rate deviates from 2.1% in only two years, namely in 1995 (2.0%) and in 1998 (2.2%). This is probably due to rounding errors.

\(^7\) This calculation is meant to be illustrative only, since the repercussions of the prolonged economic weakness on potential output are not considered. The output gap thus calculated cannot be closed immediately but rather only over a period of several years.
TFP and the NAIRU based on the following time series of the current AMECO database for the period 1970-2007 and 1970-2000, respectively: real GDP, net capital stock, labor force, standardized unemployment rate, wage share and NAIRU. The time series for West Germany and unified Germany are linked using growth rates. We then calculate the average wage share (62%) and – by rearranging the production function equation – a time series for total factor productivity (TFP). First, we apply an HP filter on the labor force and on TFP to produce their respective potential values and, subsequently, a series for potential output. Focusing again on the year 2000 we calculate an output gap of +1%. Second, we go back in time to 2001, a time when the time series above included data up to only 2000. To extend the series until 2007 we apply the two methods most commonly used by international organizations: simple ARIMA models and ad-hoc extensions. In the ARIMA version TFP and labor force are estimated in log levels, more specifically with an AR(2) model with trend and a simple AR(2) model, respectively. The new data points thus generated exceed the trend observed in 1995-2000. In contrast, the ad-hoc method extrapolates this trend. The NAIRU is in both cases generated according to the method used by the EU Commission, i.e. we increase (decrease) the NAIRU by half of the change in the preceding year. We now recalculate potential output based on these data. The time series generated by the AR model yields an output gap of 0.4% in 2000, the trend-based approach one of -0.3%.

Our example shows that potential output estimates greatly depend on the expected values of its components which, in turn, largely depend on the respective previous development in the estimation models used. It follows that current estimates of Germany’s potential output may prove to be far too pessimistic if the economic weakness of the past years proves to be a temporary phenomenon.

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8 The revisions are not the result of changes in the data provided by the Federal Statistical Office or a different interpretation of the existing wage pressure. The revisions of Germany’s growth rates for 1999, 2000 and 2001 amount to 0.5 percentage points, 0.1 percentage points and 0.7 percentage points, respectively. Although these revisions can partly explain the revisions of the output gap, they offer no grounds for downward revisions of potential output (Calculations of the authors based on data provided by the Federal Statistical Office.)
4. **IMK estimates of Germany’s potential output**

Like most international organisations we use a production function approach to estimate potential output in Germany. The NAIRU is estimated using a Kalman filter. For various reasons we stick relatively close to the modelling strategy of the EU Commission (Denis et al. 2002), one being its relevance for the national governments in the Euro Area when, for instance, formulating their stabilisation programmes. One important difference is the way in which we calculate the potential level of the components of the production function, namely the NAIRU and total factor productivity.

We estimated the following Cobb-Douglas production function:

\[ Y^*_t = A^*_t L^*_t^\alpha K^*_t^{1-\alpha}, \]

where \( Y^* \) is potential output, \( A^*_t \) potential total factor productivity, \( L^*_t \) potential hours worked, \( \alpha \) the partial elasticity of production with respect to labor and \( K^*_t \) the capital stock.

The NAIRU is needed to calculate the potential hours worked. More specifically (1-NAIRU) is multiplied with the potential labor force (HP-filtered actual labor force) to determine the non-inflation-accelerating level of employees. The latter is then multiplied with average potential working time (HP-filtered actual average working time) to calculate potential hours worked. The coefficient \( \alpha \) is equated with the average wage share in the given period (0.65). The potential capital stock is taken to be identical with the actual capital stock. Potential total factor productivity (\( A^*_t \)) is then determined by first solving the production...
function for $A$, using actual employees and actual GDP rather than their potential levels. This TFP is then estimated as dependent on several determining factors. Potential total factor productivity is calculated by plugging the potential levels of these factors into the equation. In the following we first describe the data used and then present our estimates of the NAIRU, total factor productivity, and potential output.

4.1 Data sources

We mainly use annual data provided by the German Federal Statistical Office (Destatis). These are by and large identical to the data used by the EU Commission. When this paper was written, no official time series for the German capital stock existed, so we used the EU Commission’s time series, adjusted using time series for depreciation and gross fixed investment to make it compatible with the German system of national accounts. Furthermore we use the standardized unemployment rate provided by Destatis on an annual basis, by the OECD on a quarterly basis. We deal with German unification, as does the EU Commission, by linking the time series in growth rates thus calculating (artificial) levels prior to 1992. Institutional variables used in estimating the NAIRU are taken primarily from the dataset of Nickell et al. (2001), Bassanini/Duval (2006), the OECD’s databank, Martinez-Mongay (2000, 2003), Destatis, AMECO and Visser (2006). Nickell et al. (2001) provide a time series on employment protection which we extended beyond 1995 using data from Bassanini/Duval (2006), the last two data point were estimated making adjustments for various reforms. The Nickell et al. (2001) time series on union density was extended using data from Visser (2006), the last year is our estimate based on the assumption that the decreasing trend continued. We continued the series on replacement rates provided by Bassanini/Duval (2006) with two estimated data points, taking into account that replacement rates are lower in 2005 due to the partial merging of welfare benefits and unemployment benefits (Hartz-IV reform) and that the OECD’s net replacement ratio registered a decrease for all household groups in 2004. For the wage wedge we used two different time series: the first is the absolute difference between compensation of employees and net wage sum in percent of compensation of employees (national accounts data). The second series is an updated version of the effective tax burden (taxes, duties, social security contributions) on labor as calculated by the EU Commission (Martinez-Mongay 2000 and 2003). It is the ratio of the sum of non-wage labor costs and wage tax to gross wages and salaries. The monetary indicators used to estimate the NAIRU are based on data from the German Bundesbank. The overnight rate and “indicator of the German economy’s price competitiveness against 19 countries based on the deflators of total sales” were used as provided by the Bundesbank. The real short-term interest rate is the overnight rate minus the change in the GDP deflator, the latter calculated on the basis of the Destatis time series on real and nominal GDP (before 1992: West Germany).

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10 Cf. Deutsche Bundesbank (2005: 25) for an overview of these reforms.
To estimate total factor productivity we used as additional data sources the Congressional Budget Office (U.S. potential total factor productivity), AMECO database, OECD Main Science and Technology Indicators (per capita expenditure on research and development) as well as Ifo and OECD (capacity utilization in manufacturing). ¹¹

4.2 The NAIRU

4.2.1 Kalman-filter estimate of the NAIRU

The problem with estimating the NAIRU is that it an unobservable variable. The Kalman-filter approach was developed specifically to estimate such variables and it has the advantage over univariate filter methods that it links the unemployment gap to some measure of inflation. In that sense it satisfies the definition of the NAIRU and gives the estimate economic content. In addition, it is possible to estimate the influence of exogenous factors, such as monetary policy. It should be noted, however, that the results of the Kalman-filter estimate strongly depend on the specification of the estimated equations. For example, the fact that the NAIRU is specified as an AR(2)-process implies that it is necessarily a stationary variable. Although this is a sensible assumption, it would have been preferable to find this characteristic as a result rather than plugging it in as an assumption. An alternative method based on fewer assumptions is the Elemenkov method that the OECD used until a few years ago. Unfortunately the estimated NAIRU is so volatile, that one is forced to use a HP-filter or the like to obtain a sensible time series. The HP-filtered Elemenkov NAIRU, however, is hardly distinguishable from a plain HP-filtered NAIRU, leading us to reject this approach.

To estimate the unobservable NAIRU with the Kalman filter it is necessary to make an assumption about how the NAIRU interacts with other economic variables that are observable as well as the time series properties of the NAIRU and, in this case, the output gap. We estimate the NAIRU as a nonstationary trend (time series property), more precisely as a local linear model, ¹² and assume that the unemployment gap (u-u*) significantly affects inflation. To use the information contained in this economic relation – the Phillips curve – the NAIRU is estimated simultaneously with the Phillips curve. The unemployment gap is modeled as an AR(2) process. ¹³

State equations:

\[(u-u^*)_t = a_1 (u-u^*)_{t-1} + a_2 (u-u^*)_{t-2} + \epsilon_{\text{gap}}\]

¹¹ Neither the Federal Statistical Office nor the OECD provides a long time series about the educational attainment of the population.

¹² A local linear model is de facto equivalent to a ARIMA(0,2,1). Depending on the variances of the two error terms it can be either a simple random walk or an I(2) process. Many authors use this approach because it allows for a smooth trend; cf. Harvey und Jaeger (1993).

¹³ This is a typical way of modeling the unemployment gap; cf. Fabiani/Mestre (2001) and Apel/Jansson (1999).
\[
\text{Na} \text{iru}^{\text{implizit}}_t = \text{Na} \text{iru}^{\text{implizit}}_{t-1} + \text{trend}_t + \varepsilon^{\text{na} \text{iru}}_t
\]
\[
\text{trend}_t = \text{trend}_{t-1} + \varepsilon^{\text{trend}}_t
\]
\[
\text{Na} \text{iru}_t = \text{Na} \text{iru}^{\text{implizit}}_t + \delta Z^{\text{na} \text{iru}}_t
\]

**Definition equation:**
\[
u_t = (u-u^*)_t + \text{Na} \text{iru}_t
\]

**Phillips curve equation:**
\[
\Delta^2 w^h_t = \beta (u-u^*)_t + \gamma X^{\text{Phillips}}_t + \varepsilon^{\text{phil}}_t
\]

\(X^{\text{phil}}_t\) denotes exogenous variables that affect hourly wages \((w^h)\).

First we estimate the NAIRU without exogenous variables \((\delta=0)\) similarly to EU Commission and OECD (Denis et al. 2002, Turner et al. 2001). Like the EU Commission we estimate the Phillips curve in terms of wage inflation, rather than price inflation as is the norm, so as to exclude price shocks that are unrelated to the labor market. Unlike the Commission we do not include the wage share in the Phillips curve equation. In the Commission’s estimates the wage share has great explanatory power which in our opinion is the result of an error: in deriving the Phillips curve an economic equilibrium condition is replaced by a definition. This probably gives rise to an endogeneity problem that lets the equation appear to be much better than it actually is. Our Phillips curve further differs from that of the Commission in that import and export prices enter separately. Including these variables in the Phillips curve can be justified but it is not a given that they have the same (absolute) sign which would be a prerequisite for including them as one terms of trade variable. However, these differences do not substantially affect the actual estimate of the NAIRU.

The Phillips curve is derived from standard wage and price setting curves. The price setting curve replaces the Commission’s wage demand curve for the reasons cited above. Based on a Cobb-Douglas production function the Phillips curve is specified as follows:
\[
\Delta^2 w_t = a_1 \Delta^2 \text{prodh}_t - \Delta^2 s_t - \beta (u-u^*)_t + \varepsilon_t,
\]
with \(s_t\) as supply shocks other than unit labor costs that affect prices, in our case import and export prices.

The estimation begins only in 1973 although the time series start in 1970 because the series are differenced and lags are considered. Lags of the endogenous variables are insignificant and thus not included. There is no autocorrelation, which supports the decision to estimate without lagged endogenous variables. Hourly productivity was significant only at lag one, export and import prices enter the equation without lags and – as was to be expected – with opposite signs. The results are shown in the table below. Estimates that constrained these two variables to have the same absolute value were markedly inferior.

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\(14\) The authors will provide the derivation of the Phillips curve on demand.
The coefficients can simply be read of the table because there are no lagged endogenous variables: a decline in the output gap by 1 percentage point for one year (three years) permanently lowers wage inflation by about 0.5 percentage points (about 1.4 percentage points). A permanent increase in productivity growth by one percentage point permanently raises wage inflation by 0.7 percentage points; at the same time the increase in unit labor costs is permanently lowered by 0.3 percentage points. An increase in export price inflation by 1 percentage point increases wage inflation by 0.4 percentage points, a corresponding increase in import prices lowers it by 0.1 percentage points.

The AR-coefficients of the unemployment gap imply an average cycle length of nine years. The unemployment gap is estimated with a small positive constant implying deflationary pressure. This is compatible with the three disinflationary periods during the estimation period: The increase in hourly wages diminished from 12 % in the early seventies to 5 % in the late eighties and again since the mid-nineties to nearly 0 % in 2005. The variances of the error terms are not constrained, the local linear model is therefore not a simple random walk (Fabiani/Mestre 2000 and 2001, European Commission 2002 and 2006). The residuals of the NAIRU equation exhibit no autocorrelation. The distribution of the residuals of the Phillips curve is normal, that of the state equations, however, probably not. According to our estimate the NAIRU stood at 8.1 % in 2005.
Results of the Kalman-filter estimate of the German NAIRU

Maximum likelihood equation and statistics
estimation periods: 1973-2005 (33 observations)

<table>
<thead>
<tr>
<th>Variables</th>
<th>coefficients</th>
<th>s.e.</th>
<th>t-stat</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>State equations</strong></td>
<td></td>
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<tr>
<td>$a_{1}$</td>
<td>1.264</td>
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<td>$a_{2}$</td>
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<td>0.002</td>
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<tr>
<td>$\text{Var}(\varepsilon^{\text{trend}})$</td>
<td>1.95E-04</td>
<td></td>
<td></td>
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<tr>
<td>$\text{Var}(\varepsilon^{\text{gap}})$</td>
<td>2.51-02</td>
<td></td>
<td></td>
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<td><strong>Phillips curve</strong></td>
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<tr>
<td>$(\bar{u}-\bar{u}^{*})$</td>
<td>-0.462</td>
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<tr>
<td>$d^{2}\text{prodh}_{t-1}$</td>
<td>0.658</td>
<td>0.225</td>
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<td>0.192</td>
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<tr>
<td>$d^{2}\text{pim}$</td>
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<td>0.074</td>
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<td>-2*log-likelihood</td>
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<td>$\text{Var}(\varepsilon^{\text{phillips}})$</td>
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<td><strong>residual tests</strong></td>
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<td></td>
</tr>
<tr>
<td><strong>State equations</strong></td>
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<tr>
<td>Ljung-Box Q(4) statistic</td>
<td>1.463</td>
<td>prob: 83.3%</td>
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</tr>
<tr>
<td>Jarque-Bera statistic</td>
<td>9.599</td>
<td>prob: 0.8%</td>
<td></td>
</tr>
<tr>
<td><strong>Phillips curve</strong></td>
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<tr>
<td>Ljung-Box Q(4) statistic</td>
<td>4.237</td>
<td>prob: 37.5%</td>
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</tr>
<tr>
<td>Jarque-Bera statistic</td>
<td>1.285</td>
<td>prob: 52.6%</td>
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</table>
The Commission’s GAP program allows us to include exogenous variables in estimating the NAIRU. This approach is somewhat problematic because the state equations are split into three different groups: the unemployment gap, a statistical process (here: local linear model) and the exogenous variables.\(^\text{15}\) It follows that the exogenous variables can only affect the NAIRU temporarily unless they represent structural breaks. Including lagged unemployment only partly solves the problem since the GAP program then regresses the unemployment rate rather than the NAIRU on the exogenous variables. We therefore applied this one-step Kalman-filter approach primarily when testing for hysteresis. Institutional and monetary policy variables were, in addition, tested for in a two-step approach: We first estimated the NAIRU with the Kalman filter and then used OLS to regress this NAIRU on the exogenous variables. Compared to other studies using OLS ours has the advantage of using an estimated NAIRU rather than resorting to longer term averages of the unemployment rate like, for example, Blanchard/Wolfers (2000) or forgoing degrees of freedom like Nickell et al. (2002) who include an inflation variable in the regression to exclude cyclical movement.

### 4.2.1 Exogenous variables

The effects of institutional variables on the NAIRU were tested for using four variables, namely employment protection, union density, replacement rate and wage wedge. These

\(^{15}\) An alternative approach would be to split unemployment into unemployment gap and NAIRU, the latter in turn being modeled as a function of itself (random walk approach) and the exogenous variables.
variables feature greatly in the literature, are available as long time series and largely reflect Germany’s recent labor market reforms. We included the variables in the NAIRU estimation individually and together using both the Kalman filter and OLS. With the exception of the wage wedge, the outcomes of the estimations with institutional variables were not robust, being either highly dependent on the specification of the estimated equation or insignificant or bearing the wrong (theoretically implausible) sign. In part this may be due to statistical problems arising from German unification. Furthermore, it should be noted that since the late seventies the examined variables again with the exception of the wage wedge – should have lowered the German NAIRU if they affected it at all. The limited explanatory power of institutional variables for unemployment is also pointed out in the literature (Blanchard/Katz 1997: 68, Machin/Manning 1999: 3107, OECD 2006: 214 and Bassanini/Duval 2006: 63). Blanchard/Wolfers (2000:2), for example, argue that

“...many of these institutions were already present when unemployment was low (and similar across countries), and, while many became less employment-friendly in the 1970s, the movement since then has been mostly in the opposite direction. Thus, while labour market institutions can potentially explain cross country differences today, they do not appear able to explain the general evolution of unemployment over time.”

In line with part of the literature monetary policy was also tested for as a factor that affects long-term unemployment. There is no doubt that the restrictive monetary policy in the late seventies as well as the early eighties and nineties played a big role in the increase of the unemployment rate. Whether this effect was only of a short-term nature – thus not affecting the NAIRU – is however quite controversial. If monetary policy gives rise to hysteresis in labor markets, for example, and thereby changes the effective labor supply, its short-run effects may extend to the long run. Based on Granger causality tests (Blinder/Bernanke 1992) of various monetary policy indicators and the standardized unemployment rate, we

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16 The wage wedge (based on national accounts data) was found to be significant in both the Kalman-filter estimate and the OLS-estimate. Due to possible endogeneity it was introduced with a lag. The Kalman filter finds a coefficient of 0.18 for the first lag, OLS a comparable one of 0.15. The latter changes only minimally when a different deterministic structure is used. Our results are at the lower end of the range of 0 to 0.6 found in the literature (Planas/Röger/Rossi 2006). The coefficient of 0.18 implies that 2.5 percentage points of the increase in the NAIRU between 1973 and 1998 were the result of a widening wage wedge; since 1998 the wage wedge led to a small reduction in the NAIRU of 0.3 percentage points. In contrast, the wage wedge as calculated in line with the EU Commission was insignificant.

17 Cf. Ball and Mankiw (2002), Ball (1999), Blanchard and Katz (1997) as well as Fitoussi, Jestaz, Phelps, and Zoega (2000), who relate the marked increase in unemployment and the fact that it remained high to the restrictive stance of monetary policy in Europe.

18 Modern monetary policy is based on the notion that money is not neutral in the short term. Nominal rigidities give rise to short-term non-neutrality; cf. Clarida, Gali, and Gertler (1999), McCallum (2001), Mankiw (1985), Akerlof, Dickens, and Perry (2000). In the short term monetary policy is thought to have an effect on real interest rates, aggregate demand and inflation. Unemployment is the key variable through which monetary policy affects inflation (Layard, Nickell, and Jackman 1991: 13).

19 Contrary to the mainstream view, the view that monetary policy has long-term real effects is put, for example, by Cross (1995) and Ball (1999).
used the deviation between the real short-term interest rate and the rate of economic growth. This monetary policy indicator has the advantage of being unaffected by fundamental changes in the real interest rate due, for example, to a change in the potential growth rate. It is superior to the nominal overnight rate because the effects of monetary policy are not independent of inflation: an increase in interest rates that lags behind the increase in inflation is likely to have an expansionary effect, for example. We analysed the effect of this variable in two different Kalman-filter models and one OLS regression using our Kalman-filter NAIRU. In each case the variable was significant and robust, albeit with a relatively low coefficient of 0.1. As a check we estimated an additional OLS regression in which we determined the long-term monetary policy effect on the unemployment rate directly, rather than its effect on the NAIRU. Conceptually the two are obviously identical. The stationary monetary policy indicator enters the equation in levels, the nonstationary unemployment rate in first differences. The long-term coefficient is here estimated as 0.22 and the results are robust to different specifications. Our preferred specification was derived using the general-to-specific approach and includes a trend that can be interpreted to proxy omitted variable. It exhibits no econometric problems.

The results of our hysteresis estimates are also robust. Hysteresis can have different causes but the key factor seems to be that the number of long-term unemployed increases and that these influence labour market developments and wages, in particular, less than do the temporarily unemployed. Numerous studies have found empirical evidence for hysteresis (Logeay/Tober 2006; Røed 1997). Our approach is similar to that used by Salemi (1999) and Jaeger/Parkinson (1994) and superior to unit root test (Léon-Ledesma 2002; Léon-Ledesma/McAdam 2004) cointegration (Johansen 1995), lagged unemployment in wage-price systems (Layard, Nickell, and Jackman 1991) and Markov-switching (Léon-Ledesma/McAdam 2004) because it does not require the assumption of a certain invariance of the institutional structure like unit root tests and Markov-switching nor a full specification of the determinants of the NAIRU as do cointegration and panel estimations of wage-price systems.

The time series for long-term unemployment was constructed from two sources. For the period 1983 until 2004 we used OECD data which corresponds more closely to the standardized unemployment rate than does the long-term unemployment rate provided by the Federal Employment Agency. The missing years were estimated using data from the Federal Employment Agency and IAB. Several different specifications were used to account for German unification. The best ones included a step or impulse dummy variable for 1991. In both estimations the coefficient of the rate of long-term unemployment is 1. Translated into the effect of lagged unemployment, which is often used to measure hysteresis effects, the coefficient is 0.4. Our coefficient is approximately twice as large as that in Jaeger/Parkinson (1994), who apply a similar method but use lagged unemployment and find a coefficient of 0.18 for Germany. It does, however, correspond to the coefficient in Jaeger/Parkinson (1990).
The fact that the rate of long-term unemployment proved to be significant in the estimation of the NAIRU indicates the presence of hysteresis. Hysteresis, in turn, implies that variables will affect the NAIRU if they cause unemployment to stay high or low for a prolonged period. Our analysis thus shows that the unemployment gap and the NAIRU are not independent of each other: to a certain degree the structure of unemployment hardens or loosens, thus causing the unemployment gap to close partly through an increase or decrease in the NAIRU.

### 4.2.1 Projecting the NAIRU

Projecting potential output requires that the NAIRU is projected as well. We used three different methods to forecast the NAIRU, namely the method employed by the EU Commission, the Kalman filter and an OLS equation with projected values for the exogenous variables wage wedge and monetary policy indicator. Despite the methodological differences the NAIRU projections range only from 8 % to 8.2 %. It follows that the different methods of estimating the NAIRU do not greatly affect the projection of potential output. As indicated above, this does not imply that the projection of the NAIRU is particularly accurate but rather that the statistical characteristics of the NAIRU (and the unemployment gap) – which are identical in all the cases presented here – dominate the results.

It should be noted that the statistical characteristics dominate not only the projection of the NAIRU but also its estimation: The Kalman-filter estimate of the NAIRU using a fictitious constant inflation rate for the estimation period yields a time series for the NAIRU that hardly differs from the estimate above. Similarly, the use of a univariate Kalman filter only changes the results by 0.5 % or 0.7 %, depending on the specification used. The chart below shows that the NAIRU estimate is affected more by whether it is modeled as a random walk or as a local linear model than by whether a univariate or a multivariate model is used. There is a difference in the level of the NAIRU, the movement in NAIRU is almost identical, so that although the output gap is affected the effect on potential growth is non-existent.
Univariate and multivariate Kalman-filter estimates of the NAIRU

4.4 Estimate and projection of potential total factor productivity

Potential total factor productivity (TFP*) is the second key variable to be estimated to determine potential output in the production function approach. Unlike the EU Commission (Denis et al. 2005, Carone et al. 2006) we estimated an equation that allows for the total factor productivity to be partly determined by other economic variables, namely the investment ratio, per-capita expenditure on research and development and U.S. total factor productivity.

Because there are only 30 data points we estimated specific to general rather than vice versa. The estimate is in levels although the variables are nonstationary. This is permissible because sufficient lags of each variable are included. An increase in the investment ratio by
1 percentage point is estimated to increase total factor productivity by 1.2%. An increase in expenditure on research and development (per capita) by 1% raises the TFP by barely 0.1%. An increase in U.S. TFP by 1% increases German TFP by 0.9%. We also find monetary policy to have an effect, albeit an indirect one via the investment ratio. An OLS regression with the investment ratio in first differences as dependent variable and the monetary policy indicator as independent variable yields an elasticity of -0.1. According to this estimate a three-year monetary restriction keeping the real overnight rate 1 percentage point above the growth rate of GDP, would permanently lower the investment ratio by 0.3 percentage points.

Potential TFP was determined by plugging equilibrium values for the investment ratio and research and development expenditure into the TFP equation. We defined the equilibrium investment ratio as the average investment ratio during the observation period (21.7%) which roughly corresponds to the recent investment ratios in the other countries of the Euro Area. The equilibrium path for research and development expenditure was generated with a broken deterministic trend. We distinguished between 4 phases: the seventies with annual per-capita R&D expenditure exceeding 10%, the eighties when the growth rate was almost half as high; the unification years which saw a decline in the absolute level, and the period since 1995 with relatively low growth rates of 4 to 5%. For US TFP we took the actual levels, because these are assumed to be unaffected by developments in Germany.

Actual, explained and potential TFP

1 Actual TFP is calculated by rearranging the production function, explained TFP is estimated using three exogenous variables and potential TFP is the estimate of TFP with the investment ratio and R&D expenditure in equilibrium.
There are different methods for forecasting potential TFP. The EU Commission uses a univariate model to estimate and forecast actual TFP and then an HP-filter to generate an estimate and forecast of potential TFP. Our approach differs in that we use the OLS regression to project potential TFP. The potential investment ratio is again assumed to be 21.7%, the potential increase of per-capita R&D expenditure 4.6% which corresponds to the average of the period 1995 to 2004. For the US TFP we use the CBO’s forecast of 1.4% (CBO 2006). According to the forecast of the EU Commission potential TFP will increase at an annual rate of 0.8%, the AR model yields 1.5% and our OLS regression forecasts an annual increase in potential TFP of 1.7%. It is important to note that in the production function TFP translates one to one into potential output.

4.6 Estimating and projecting potential output

Given the estimates and projections of the NAIRU and TFP we estimated potential output using the following equation:

\[ Y_t^* = TFP_t^* \times (\text{laborforce}_t^* \times \text{working time}_t^* [1-\text{Nairu}])^{0.65} (K_t)^{1-0.65} \]

Estimates of the German output gap using several NAIRUs and several potential TFPs

The substantial differences between the estimates arise primarily from the different series for potential TFP. At the end of the estimation period our estimates show large negative output gaps resulting from the fact that the recent slowdown in economic activity is not attributed to a change in potential output growth.

Potential output was then projected using the following equation: \[ Y_t^* = TFP_t^* \times (\text{labor force}_t^* \times \text{working time}_t^* [1-\text{Nairu}])^{0.65} (K_t)^{1-0.65} \]. As we have several versions of the NAIRU and
potential TFP we show an upper, lower and middle version. The upper version is based on estimated equations of potential TFP and the NAIRU, the middle version on AR models and the lower version on the respective methods used by the EU Commission. The capital stock is determined endogenously based on the potential investment ratio of 21.7%. In accordance with its definition the capital stock is calculated as follows.

\[ K_t = K_{t-1} + (\text{gross fixed investment} - \text{depreciation}) \]

To project the capital stock the equation is rewritten using the equilibrium investment ratio and a depreciation rate of 4.71%:

\[ K_t^{\text{forecast}} = \left[ 1/(1-\text{depreciation rate}) \right] \left[ K_{t-1}^{\text{forecast}} + \text{investment ratio} \times Y_t \right]. \]

Combined with the equation for \( Y_t^{\star} \), this is a system that can be solved. The results are shown in the following chart.

**Potential output: different versions**

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All estimates are based on HP filters of the labor force and working time with forecasts until 2010.

Estimation differences result primarily from the following: For the observation period (1970-2005) there is only one source for differences, namely the methods for calculating potential TFP. The blue line is based on the OLS regression of potential TFP with the exogenous variables (exception: US TFP) in equilibrium. The orange and red lines reflect a simple HP filter of TFP; different paths in the forecast period also affect the observation period, especially 2005) because of the endpoint problem. All estimates have the same NAIRU in the observation period, not however in the forecast period. The upper, middle and lower versions of
potential output growth imply an annual increase of 2.4 %, 2.1 % and 1.3 %, respectively, for the period from 2006 to 2010.

Both NAIRU and potential TFP greatly affect the estimate of potential output. Potential TFP varies substantially depending on how the equation is specified. The effect of TFP on estimation differences of potential output is greater for two reasons: first, TFP estimates, and more specifically the increase in TFP, differ more greatly than NAIRU estimates and second, there is a one-to-one correspondence between potential TFP and potential output in the production function. The NAIRU although relatively robust ultimately depends to a large extent on the assumed econometric properties of both the NAIRU itself and the unemployment gap. Furthermore, estimates and forecasts of the labour force and hours worked are highly uncertain. The effect of the NAIRU on potential output is given by the elasticity of labor. In other words a decline in the NAIRU by one percentage point raises potential output by approximately 0.7 %. Therefore a decline of the German NAIRU by 4 percentage points to 5 % would increase potential output by 3 % or stretched over a period of three years by annually 1 %.

5. Conclusion

The ultimate lack of knowledge about the precise values of the NAIRU and potential total factor productivity allow for the estimation of many different levels of potential output. It is therefore extremely problematic to use this theoretically compelling concept as a basis for economic policy advice. Furthermore, most macroeconometric models explicitly assume a long-run neutrality of money. If this assumption is false, as contended both from a theoretical and empirical perspective in the literature (Cross 1995, Solow 2000; Ball/Mankiw 2002), then low potential growth may become a self-fulfilling prophecy. Labor market hysteresis is one channel of long-run monetary non-neutrality, a lower investment ratio and thus lower TFP growth another. The OECD further notes that long-lasting periods of economic expansion give rise to increasing participation rates (OECD 2006: 49), i.e. an increasing labor supply.

A crucial aspect of German economic development since 2000 is that the end of the upswing in mid-2000 was not the result of an overutilization of productive capacity and a resulting economic policy reaction. Although at 3.3 % the increase in hourly wages was faster than in the years before (and after), it was actually just right from a macroeconomic perspective only in that year. Given the ECB’s target inflation rate of about 1.9 % and an average medium-term increase in productivity by 1.5 % p.a. the productivity-oriented increase of hourly wages lies at 3.4 % – and this rate is relatively low because it is based on the average productivity increase during the economic slump of 2000-2005. Unit labour costs in 2000 increased at a rate of only 0.7 % and thus had a dampening effect on inflation. This can
hardly be interpreted as a sign of overheating.\footnote{The fact that inflation in Germany reached 2\% in 2001 was primarily the result of the drastic oil price hike and the increase in food prices due to two animal diseases – unit labour costs rose by only 0.6\% in 2001 (Federal Statistical Office).} It follows that OECD and International Monetary Fund in spring of 2001 estimated the German output gap to be at -1.0\% and -0.9\%, respectively. In retrospect from the year 2006 the year 2000 is now interpreted to be a year of marked capacity overutilization: OECD and International Monetary Fund in retrospect estimate the output gap to have been decidedly positive, at +1.8\% and +1.7\%, respectively. This drastically revised interpretation of the business cycle is not due to a reinterpretation of the wage pressure or of the actual increase of GDP in 2000 and the years before, but rather to the methods used to estimate potential output. As discussed, these methods rely heavily on the most recent past. The economic weakness since 2000 has therefore led to a downward revision of potential output (growth). The main reason for the economic downturn was an inappropriate macroeconomic policy reaction to a series of adverse exogenous shocks since 2000.\footnote{To be named first and foremost are the oil price shock and the international collapse of stock prices at the beginning of the decade, but also the US recession, the terror acts of 9/11 and the geopolitical uncertainties relating to the war in Iraq as well as the further increase in oil prices well into the year 2006.} Had fiscal policy, in particular, reacted in an appropriate expansionary manner, German growth in 2001-2005 could have been significantly higher than the actual annual average of 0.6\% given an average increase in unit labour costs of only 0.1\% (Hein et al. 2005). Accordingly, unemployment rate and NAIRU would not have increased but rather fallen. The common methods of calculating potential output would have responded to higher growth by showing correspondingly higher potential growth rates.

Using the production function approach it is possible to identify factors that positively affect potential output, as for example, the investment ratio. But no estimate of potential output can be claimed to be accurate or precise and estimates for a given period vary significantly over time. This, however, vastly complicates fiscal planning and the use of monetary policy rules, such as the Taylor rule. Policy makers cannot rely on actual figures presented since they may change the following period. The bottom line is that potential output as measured by the methods presently available cannot be considered as a yardstick for economic policy theory.

In the literature there are three key proposals to deal with the uncertainty of potential output estimates. The first is based on Orphanides/Williams (2002) and argues that economic policy should be oriented towards GDP growth rates instead of the output gap (or changes in the unemployment rate rather than the unemployment gap). The second, closely related proposal recommends that economic policy makers quantify potential growth and thus the output gap conservatively, i.e. rather too small than too large (European Commission 2002: 9). Both proposals essentially imply that the status quo – the existing trend – is reinforced. Furthermore, both may provoke excessive policy reactions (Yellen 2002: 132f.). Focussing on the status quo and restrictive macro policy have even more serious implications if macro
policy is not (super-) neutral in the long run but rather affects not only GDP but also potential output, via hysteresis effects for example. Therefore we find the third proposal superior that argues for giving uncertain output gaps less weight in monetary policy decisions (Smets 1998, Meyer 2000 and Orphanides/Williams 2002). We argue, however, that whilst economic policy should disregard output gap estimates, it should nonetheless act preemptively by keeping a close eye on wage costs and, in particular, unit labour costs. Unit labour costs are a good indicator for underlying inflation which, in turn, provides information about the under- or overutilization of capacity (Fagan et al. 2001; Duong et al. 2005: 35). For fiscal policy the lack of reliable output gap estimates would be less problematic if its focus were on longer term expenditure paths rather than structural deficits (Horn/Truger 2005).

Given the difficulties involved in robustly estimating potential output, economic policy makers need to learn to pursue their policy objectives without reference to this variable. Pragmatism should prevail. In the face of a benign inflation outlook and high unemployment economic policy should strive to test the limits of potential output and to set in motion a virtuous cycle of a decreasing NAIRU, a rising participation rate, higher productivity growth and an improvement in fiscal balances.
6. Literature


Duong, M./Logeay, C./Stephan, S./Zwiener, R. with the collaboration of Serhiy Yahnych, Modelling European Business Cycles (ECB Model), DIW Berlin, Data Documentation 5, 2005, Berlin


International Monetary Fund: World Economic Outlook, September, several spring issues.


OECD: Economic Outlook, Paris, several spring issues.


